## NAME:

## Abstract Algebra Math 521A Michael E. O'Sullivan

## Review for first exam

- Be able to state accurately and precisely these main theorems:
  - Division theorem;
  - The gcd of two integers may be written as a linear combination of them;
  - Unique factorization.
- Know how to:
  - Prove fundamental results about divisibility.
  - Use the Euclidean algorithm to find a gcd, and to express the gcd as a linear combination.
  - Compute in  $\mathbb{Z}_n$  (don't forget to simplify!).
  - Find the inverse of an element of  $\mathbb{Z}_n$ , when possible (Euclidean algorithm or trial and error).
  - Given  $a \in \mathbb{Z}_n$ , find  $b \in \mathbb{Z}_n$  such that ab = 0, when possible.
  - Prove every nonzero element of  $\mathbb{Z}_n$  is either a zero divisor or a unit.
  - Find solutions to an equation in  $\mathbb{Z}_n$ , by trial and error, or by using inverses, or zero divisors.