Abstract Algebra<br>Math 521A<br>Michael E. O'Sullivan<br>Review for first exam

- Be able to state accurately and precisely these main theorems:
- Division theorem;
- The gcd of two integers may be written as a linear combination of them;
- Unique factorization.
- Know how to:
- Prove fundamental results about divisibility.
- Use the Euclidean algorithm to find a gcd, and to express the gcd as a linear combination.
- Compute in $\mathbb{Z}_{n}$ (don't forget to simplify!).
- Find the inverse of an element of $\mathbb{Z}_{n}$, when possible (Euclidean algorithm or trial and error).
- Given $a \in \mathbb{Z}_{n}$, find $b \in \mathbb{Z}_{n}$ such that $a b=0$, when possible.
- Prove every nonzero element of $\mathbb{Z}_{n}$ is either a zero divisor or a unit.
- Find solutions to an equation in $\mathbb{Z}_{n}$, by trial and error, or by using inverses, or zero divisors.

