## DISCRETE MATHEMATICS Math 245 Michael E. O'Sullivan

Suggestions for Preparing for the Final Exam

I. Understand fundamental logic.

- Truth tables for  $\land$ ,  $\lor$ ,  $\Longrightarrow$ , xor.
- Know how to negate a statement (Important!).
- II. Know the statements of the following theorems:
  - Quotient-remainder theorem.
  - The unique factorization theorem.

IV. Know the basics of set theory!

- Subset. Intersection, union, set difference, complement.
- Power set, Cartesian product, partition.
- Relation, inverse of a relation, function. Injective (one-to-one), surjective (onto) and bijective functions.
- Reflexive, symmetric, antisymmetric, asymmetric, transitive.
- Equivalence relation, equivalence class.
- Partial order (poset). For posets, maximal, minimal, least, greatest.

V. Know your relations.

- Know how to use tables, graphs and lists of elements to represent a relation.
- Verify or prove that a relation R is reflexive (ditto for reflexive, transitive, equivalence relation, partial order).
- For a relation R on A, be able to find the smallest relation containing R which is symmetric (ditto for reflexive, transitive, an equivalence relation, a partial order).
- Know the standard examples of equivalence relations (mod n, 10.3.10 and exercises 10.3 #18, 19, 22, 23).
- Know the standard examples of partially ordered sets:  $\leq$  for the integers (or rationals) divides on the integers;  $\mathcal{P}(\mathcal{A})$  for a set A;  $D_n$ ; (10.5 #16, 17, 18, 19, 20).
- Draw Hasse diagrams for a poset. Find minimal and maximal elements of a poset.

VI. Functions as relations.

- Determine when a relation is a function, and if so, when it is injective, surjective, or bijective.
- Find the inverse relation of a function. Is it a function, injective, surjective?
- Give examples of functions satisfying various properties (7.2 # 8, 9, 12, 13).

VII. Know the basics of recursion and induction!

- State the well-ordering principle.
- State the principle of induction.
- Be able to use summation and product notation.
- Find the first several terms of a sequence given the initial terms and the recurrence formula.

VIII. Know the formulas for the following sums:

- The sum of a geometric sequence.
- The sum of the first n integers.

IX. Know how to prove by induction!

- Use full sentences.
- State the predicate.
- Prove the base step.
- State the assumption for the inductive step.
- Given the initial terms and the recurrence formula for a sequence and given a formula for the nth term as a function of n prove that the latter is correct.

X. Know how to count!

- Poker hands (I will describe the hand, and I may give you a strange deck).
- State the binomial theorem, and use it to find a particular coefficient in a binomial expansion (6.7 #4- 8).
- Know the 4 ways to choose and the formulas for 3 of them (I won't test order unimportant, repetition allowed).